

Inference at * 2 2

of proof for Lemma p-fun-exp-add-sq:

1. $A : \text{Type}$
 2. $f : A \rightarrow (A + \text{Top})$
 3. $x : A$
 4. $m : \mathbb{Z}$
 5. $0 < m$
 6. $\forall n:\mathbb{N}. (\uparrow \text{can-apply}(f^{\wedge} m - 1; x)) \Rightarrow ((f^{\wedge} n + (m - 1)(x)) \sim (f^{\wedge} n(\text{do-apply}(f^{\wedge} m - 1; x))))$
 7. $n : \mathbb{N}$
 8. $\uparrow \text{can-apply}(f^{\wedge} m; x)$
 9. $\neg(n = 0)$
- $\vdash (f^{\wedge} n + m(x)) \sim (f^{\wedge} n(\text{do-apply}(f^{\wedge} m; x)))$
by ((Unfold 'p-fun-exp' (0)·)
CollapseTHEN (RecUnfold 'primrec' 0)·)
CollapseTHEN (
 ((RepeatFor (first_nat 3:n) (((if (0) =0 then SplitOnConclITE else SplitOnHypITE (0))·)
CollapseTHEN (Auto·)·))·)
CollapseTHEN (((Try ((Complete (Auto')·)·)·)
CollapseTHEN ((Reduce 0)
CollapseTHEN (Fold 'p-fun-exp' 0)·)·)·)
- 1:
10. $\neg(n+m = 0)$
 11. $\neg(n = 0)$
 12. $\neg(m = 0)$
- $\vdash (f \circ f^{\wedge} (n+m) - 1 (x)) \sim (f \circ f^{\wedge} n - 1 (\text{do-apply}(f \circ f^{\wedge} m - 1 ; x)))$